

**After the exam of 21.06.2016:
Typical errors, comments etc.**

At most 40 points (rather than 35) are given per question.

QUESTION 1

PARTIAL SUCCESS: A valid proof of the condition $\nabla f(x_0) = 0$ (but the goal is not reached).

REWARD: 25 points.

CLARIFICATION: the condition is necessary and not sufficient.

QUESTION 2

PARTIAL SUCCESS: A valid proof that the graph of f has area 0 (but the goal is not reached).

REWARD: 25 points.

CLARIFICATION: the condition is necessary and not sufficient for integrability; see 4c3 for a simple counterexample.

PARTIAL SUCCESS: A valid proof that the boundary of $\varphi(B)$ has area 0 (but the goal is not reached).

REWARD: 30 points.

CLARIFICATION: you still need to prove that f is continuous almost everywhere.

REMARK: the graph is only a part of the boundary (unless the function is continuous).

REMARK: do not confuse continuity of the mapping $(x, y) \mapsto (x, y - f(x))$ with continuity of the function $(x, y) \mapsto \mathbb{1}_B(x, y - f(x))$.

QUESTION 3

FATAL ERRORS:¹

$$(h_1x_1 + \cdots + h_nx_n)^2 = h_1^2x_1^2 + \cdots + h_n^2x_n^2;$$

$$\langle h_1, x \rangle \langle h_2, x \rangle = \langle h_1, h_2 \rangle \langle x, x \rangle.$$

QUESTION 4

ERROR: wrong explanation (or no explanation) of the coefficient “2”: 5 points.

¹It means, no points for this question!

GRADES STATISTICS

Total	Question 1	Question 2	Question 3	Question 4
120		40	40	40
120	40		40	40
105		25	40	40
95	25	30		40
80	0	40		40
80	0		40	40
80	0		40	40
75	0		40	35
75	25	15		35
70		0	30	40
70	15	25		30
65	25			40
65	25	0		40
65		25	0	40
60		25	30	5
60		20	20	20
60	10	10		40
60	0		27	33
47	0	7	40	
45	0	10		35
45		15	15	15
43	33	10	0	
	and so on...			